

# Boolean Rules

## Associative Rules:

$$(p \ \&\& \ q) \ \&\& \ r = p \ \&\& \ (q \ \&\& \ r)$$
$$(p \ || \ q) \ || \ r = p \ || \ (q \ || \ r)$$

## Distributive Rules:

$$p \ \&\& \ (q \ || \ r) = (p \ \&\& \ q) \ || \ (p \ \&\& \ r)$$
$$p \ || \ (q \ \&\& \ r) = (p \ || \ q) \ \&\& \ (p \ || \ r)$$

## Idempotent Rules:

$$p \ \&\& \ p = p$$
$$p \ || \ p = p$$

## Double Negation:

$$!!p = p$$

## DeMorgan's Rules:

$$\neg (p \ \&\& \ q) = \neg p \ || \ \neg q$$
$$\neg (p \ || \ q) = \neg p \ \&\& \ \neg q$$

## Commutative Rules:

$$p \ \&\& \ q = q \ \&\& \ p$$
$$p \ || \ q = q \ || \ p$$

## Absorption Rules:

$$p \ || \ (p \ \&\& \ q) = p$$
$$p \ \&\& \ (p \ || \ q) = p$$

## Bound Rules:

$$p \ \&\& \ 0 = 0$$
$$p \ \&\& \ 1 = p$$
$$p \ || \ 1 = 1$$
$$p \ || \ 0 = p$$

## Negation Rules:

$$p \ \&\& \ (\neg p) = 0$$
$$p \ || \ (\neg p) = 1$$